

# A review about transportation and Vehicle Routing Problem

Mohammadreza Shahriari, Mohammad Hesam Asoodeh

Associate Professor & Faculty of industrial management, South Tehran Branch, Islamic Azad University, Tehran, Iran

Ph.D. candidate, Department of Technology Management, Islamic Azad University, Dubai, UAE

## Abstract:

This paper presents a comprehensive review of transportation management and the Vehicle Routing Problem (VRP). Transportation is an essential component of modern society, facilitating the movement of people and goods. Effective transportation management is crucial for optimizing resources, reducing costs, and improving overall system efficiency. The VRP, a combinatorial optimization problem, focuses on determining the most efficient routes for a fleet of vehicles to deliver goods or services to a set of customers, while considering various constraints. The review begins by providing an overview of transportation management, highlighting its significance in enabling economic activity and social connectivity. It explores the challenges faced in transportation systems, such as minimizing costs, meeting customer demands, and considering environmental sustainability. The role of emerging technologies, such as real-time data collection and IoT, is discussed in the context of enhancing transportation management practices.

**Keywords:** Transportation, Vehicle Routing Problem, Time Window, Optimization, Solution.

**DOI:** [10.24297/j.cims.2023.1.35](https://doi.org/10.24297/j.cims.2023.1.35)

---

## 1. Introduction

Transportation plays a vital role in our modern society, enabling the movement of people and goods from one place to another efficiently and conveniently. From daily commutes to the delivery of goods across vast distances, transportation systems are the lifeblood of economic activity and social connectivity. As our world becomes increasingly interconnected, the need for effective transportation management becomes even more critical. One key challenge in transportation management is the optimization of vehicle routing. The Vehicle Routing Problem (VRP) is a well-known combinatorial optimization problem that seeks to determine the most efficient routes for a fleet of vehicles to deliver goods or provide services to a set of customers. The objective is to minimize costs, such as fuel consumption, vehicle wear and tear, and travel

time, while satisfying various constraints, including capacity limitations, time windows, and customer demands.

The VRP has a wide range of practical applications, including package delivery, waste collection, public transportation planning, and logistics operations. Solving the VRP efficiently has significant implications for businesses and organizations, as it can lead to cost savings, improved customer satisfaction, and reduced environmental impact [1],[2],[3].

Over the years, researchers and practitioners have developed numerous algorithms and approaches to tackle the VRP. These range from exact methods, such as mathematical programming and branch-and-cut algorithms, to heuristic and metaheuristic techniques like genetic algorithms, ant colony optimization, and simulated annealing. Advances in computing power and optimization algorithms have significantly contributed to finding near optimal or optimal solutions for real-world VRP instances, considering complex constraints and dynamic environments.

Moreover, with the advent of new technologies such as real-time data collection, GPS tracking, and the Internet of Things (IoT), transportation systems are becoming smarter and more interconnected. These innovations offer opportunities to address the VRP in real-time, dynamically adapting routes and schedules based on changing conditions and demand patterns.

In this context, the study of transportation and the Vehicle Routing Problem continues to be a vibrant field of research, attracting the attention of academicians, industry professionals, and policymakers alike. By understanding the underlying principles of transportation management and developing efficient solutions for the VRP, we can unlock new possibilities for enhancing the efficiency, sustainability, and reliability of our transportation networks.

In this article, we will explore the fundamentals of transportation management and delve into the intricacies of the Vehicle Routing Problem. We will discuss various solution approaches, highlight real-world applications, and examine the potential impact of emerging technologies. Through this exploration, we aim to gain insights into the challenges and opportunities in transportation management, paving the way for smarter and more efficient transportation systems in the future [4],[5].

## 2. Transportation History

Transportation history is a fascinating and diverse subject that encompasses the evolution of human mobility and the development of various transportation modes throughout different eras and civilizations. From ancient times to the modern era, transportation has played a vital role in shaping societies, economies, and the way people connect with one another [6],[7],[8],[9]

### Early Human Transportation:

Human transportation traces back to prehistoric times when early humans relied on their own physical capabilities to move from one place to another. Walking was the primary mode of transportation, allowing humans to explore new territories, search for resources, and migrate to different regions.

### Animal-Powered Transportation:

As civilizations emerged, humans began domesticating animals for transportation purposes. The use of animals such as horses, oxen, camels, and elephants revolutionized travel and trade. Animals provided greater speed, carrying capacity, and endurance, enabling humans to cover longer distances and transport goods more efficiently.

### Water Transportation:

The development of water transportation was a significant milestone in human history. Rivers, lakes, and oceans provided natural channels for trade and exploration. Early watercraft, such as rafts, canoes, and boats, allowed humans to navigate water bodies and facilitated the exchange of goods and ideas between different cultures. The invention of sails and oars further enhanced the speed and efficiency of water transportation.

### Land Transportation:

The invention of the wheel marked a significant turning point in land transportation. Wheeled vehicles, initially drawn by animals, revolutionized the movement of people and goods. Ancient civilizations like Mesopotamia, Egypt, and China developed sophisticated road networks to facilitate trade and communication. The Roman Empire constructed an extensive system of paved roads, known as the Roman road network, which greatly improved land transportation across their vast territories.

#### Industrial Revolution and Steam Power:

The Industrial Revolution in the 18th and 19th centuries brought significant advancements in transportation technology. The introduction of steam power revolutionized both land and water transportation. Steam-powered locomotives replaced horse-drawn carts and transformed railways into a crucial mode of transport for both passengers and goods. Steamships replaced sailing vessels, providing faster and more reliable transportation across oceans, and expanding global trade.

#### Automobiles and Aviation:

The late 19th and early 20th centuries witnessed the emergence of two transformative transportation modes: automobiles and aviation. The invention of the internal combustion engine paved the way for the mass production of automobiles, making personal transportation accessible to the general population. Automobiles revolutionized urban mobility, influenced urban planning, and spurred the growth of the automotive industry. Meanwhile, the Wright brothers' successful flight in 1903 marked the birth of aviation. The development of aircraft and the subsequent growth of commercial aviation transformed long-distance travel and made the world more interconnected. Air travel became faster, safer, and more convenient, enabling people to reach distant destinations in a fraction of the time.

#### Modern Transportation and Future Prospects:

Today, transportation continues to evolve at an unprecedented pace. Technological advancements have given rise to high-speed trains, electric vehicles, maglev trains, and autonomous vehicles. The focus on sustainability has led to the development of greener transportation alternatives, such as hybrid and electric cars, and the exploration of renewable energy sources for powering transportation.

Furthermore, the concept of hyperloop, a proposed mode of transportation using near-vacuum tubes to transport people and goods at high speeds, offers a glimpse into the potential of future transportation systems.

In conclusion, transportation history is a testament to human ingenuity and the quest for faster, more efficient, and interconnected modes of mobility. From humble beginnings with walking and animal-powered transportation to the advent of automobiles, airplanes, and cutting-edge technologies, transportation has continually shaped societies, economies, and human progress.

The ongoing advancements and innovations in transportation hold the promise of even more exciting developments in the future, transforming the way we travel and connect with the world around.

### 3. Background classification

Research in the field of transportation problems can be classified into various categories based on different perspectives and objectives. Here are some common types of research conducted in the field of transportation:

**Optimization and Operations Research:** This type of research focuses on developing mathematical models, algorithms, and optimization techniques to solve transportation problems efficiently. It involves studying various aspects like route optimization, vehicle scheduling, network design, inventory management, and supply chain optimization.

In Optimization and Operations Research approaches applied to transportation problems, various variables and parameters are considered to formulate and solve the problem effectively. Here are the key variables and parameters typically considered: [10],[11],[12],[13],[14].

**Decision Variables:** These variables represent the quantities or values to be determined in the transportation problem. The primary decision variables include:

- **Allocation Variables:** These variables represent the amount of flow or quantity to be transported between sources and destinations. They indicate how much of a particular commodity or resource is moved from one location to another.
- **Routing Variables:** These variables represent the selection of routes or paths for transportation. They determine the specific sequence of nodes or links that a vehicle follows to transport goods from the source to the destination.

**Objective Function:** The objective function defines the goal of the optimization problem. In transportation problems, the objective function is typically designed to minimize or maximize a certain criterion, such as minimizing total transportation costs, minimizing travel time, maximizing resource utilization, or maximizing customer satisfaction.

**Constraints:** Constraints are conditions or limitations that must be satisfied in the transportation problem. They include:

- **Supply Constraints:** These constraints represent the availability or limitation of resources at the source nodes. They ensure that the total supply of goods from all sources does not exceed the available quantity.
- **Demand Constraints:** These constraints represent the demand or requirement at the destination nodes. They ensure that the total demand at all destinations is met and does not exceed the required quantity.
- **Capacity Constraints:** These constraints represent the capacity limitations of transportation vehicles or links. They ensure that the flow of goods on each route or link does not exceed its maximum capacity.
- **Balance Constraints:** These constraints ensure that the total supply is equal to the total demand, guaranteeing that the transportation problem is balanced.
- **Non-negativity Constraints:** These constraints enforce that the decision variables must be non-negative, indicating that the quantities transported, or routes chosen cannot be negative.

**Transportation Costs:** The costs associated with transportation play a crucial role in optimization models. These costs include transportation fees, fuel costs, labor costs, handling costs, tolls, and any other relevant expenses incurred during transportation.

**Distance or Time Matrix:** The distance or time matrix represents the distances or travel times between source-destination pairs or between different nodes in the transportation network. It is used to calculate the cost or time required for transportation and to determine the optimal routes.

**Additional Parameters:** Depending on the specific context of the transportation problem, additional parameters may be considered. These parameters could include vehicle capacities, service levels, time windows, penalty costs, vehicle availability, time constraints, and any other relevant factors that impact the optimization process.

By incorporating these variables and parameters into an optimization model, researchers can formulate the transportation problem as a mathematical programming or network optimization problem and use various techniques to find the optimal solution.

### Traffic Flow Analysis

Research in this area aims to understand and analyze the behavior and characteristics of traffic flow. It involves studying traffic patterns, congestion, traffic modeling, traffic control systems, and intelligent transportation systems. The objective is to improve traffic management, reduce congestion, and enhance overall transportation efficiency.

In Traffic Flow Analysis approaches applied to transportation problems, various variables and parameters are considered to analyze and model the behavior of traffic flow. Here are the key variables and parameters typically considered: [15],[16]

**Flow Variables:** These variables represent the characteristics of traffic flow and its components. The primary flow variables include:

**Traffic Volume:** It represents the number of vehicles passing through a particular section of the road or network within a specific period. Traffic volume is often measured in vehicles per hour or vehicles per day.

**Traffic Density:** It represents the number of vehicles occupying a given length of the road or network at a specific time. Traffic density is usually measured in vehicles per unit length, such as vehicles per kilometer.

**Traffic Speed:** It represents the average speed at which vehicles are moving through the road or network. Traffic speed is typically measured in kilometers per hour or miles per hour.

**Flow Relationships:** These relationships describe the interdependencies between flow variables and are used to model traffic flow behavior. The primary flow relationships include:

**Fundamental Diagram:** It represents the relationship between traffic flow (volume or density) and traffic speed. It characterizes how flow variables change as traffic conditions vary, such as the flow-density relationship, flow-speed relationship, or speed-density relationship.

**Flow-Delay Relationship:** It represents the relationship between traffic flow and travel time or delay. It describes how increasing traffic volume or density affects travel time and congestion.

#### 4. Traffic Control Parameters

These parameters represent the factors that influence traffic flow and are controlled to manage and regulate traffic. The primary traffic control parameters include:

**Traffic Signals:** Parameters related to traffic signal timings, cycle lengths, green times, and phasing. These parameters are crucial for controlling traffic at intersections.

**Speed Limits:** Parameters related to the maximum allowable speeds on different road sections. Speed limits are important for maintaining safety and managing traffic flow.

**Lane Configuration:** Parameters related to the number of lanes, lane width, lane markings, and lane assignments. Lane configurations influence traffic flow and capacity.

**Network Topology,** the network topology represents the spatial arrangement of roads, intersections, and links in the transportation network. It includes the connectivity between different nodes, the lengths of road segments or links, the types of intersections, and the hierarchy of roads. Network topology plays a vital role in modeling traffic flow and simulating traffic behavior.

**Traffic Demand:** Traffic demand represents the travel demands of vehicles in the transportation network. It includes origin-destination (O-D) pairs, trip generation rates, trip distribution patterns, and traffic patterns during different times of the day or week.

**Behavior Parameters:** These parameters represent the behavioral characteristics of drivers and their decision-making processes. These parameters can include factors like driver response time, lane-changing behavior, car-following behavior, route choice behavior, and driver perception and reaction characteristics.

By considering these variables and parameters, researchers can analyze and model traffic flow to understand congestion patterns, evaluate traffic management strategies, optimize traffic signal timings, study the impacts of infrastructure changes, and develop intelligent transportation systems for efficient traffic management and control [17],[18].

## 5. Transportation Planning



This type of research focuses on long-term strategic planning for transportation systems. It involves analyzing transportation needs, forecasting future demands, evaluating infrastructure requirements, and developing policies and plans to meet those needs. Transportation planning research often considers factors like land use, environmental impact, sustainability, and multimodal transportation integration.

In the Transportation Planning approach applied to transportation problems, various variables and parameters are considered to analyze, forecast, and plan for transportation systems. Here are the key variables and parameters typically considered:

**Transportation Demand Variables:** These variables represent the travel demands and characteristics of users in the transportation system. The primary demand variables include:

**Trip Generation:** It represents the number of trips originating from different zones or areas within a transportation network. Trip generation is influenced by factors such as population, employment, land use patterns, and socioeconomic factors.

**Trip Distribution:** It represents the patterns of travel between origin and destination zones within the transportation network. Trip distribution considers factors such as travel distances, travel times, transportation modes, and transportation costs.

**Modal Split:** It represents the distribution of trips among different transportation modes, such as private vehicles, public transit, walking, cycling, or other modes. Modal split is influenced by factors such as travel distances, travel times, costs, availability of transportation modes, and user preferences.

**Land Use Variables:** These variables represent the characteristics of land use and its influence on transportation demand. The primary land use variables include:

**Residential Density:** It represents the number of housing units or population density in different zones. Residential density affects trip generation rates and transportation demand.

**Employment Density:** It represents the number of jobs or employment density in different zones. Employment density influences trip generation rates, trip distribution patterns, and transportation demand.

**Land Use Mix:** It represents the diversity and proximity of different land uses (e.g., residential, commercial, industrial) within a transportation network. Land use mix affects trip lengths, trip distribution patterns, and transportation mode choices.

**Infrastructure Parameters:** These parameters represent the physical characteristics and capacity of transportation infrastructure. The primary infrastructure parameters include:

**Road Network:** Parameters related to the road network, such as road lengths, connectivity, road classifications, number of lanes, road geometries, and road capacities.

**Public Transit Network:** Parameters related to public transit systems, such as transit routes, transit stops or stations, service frequencies, vehicle capacities, and transit network connectivity.

**Bicycle and Pedestrian Infrastructure:** Parameters related to bicycle and pedestrian infrastructure, such as bike lanes, sidewalks, crosswalks, pedestrian bridges, and cycling or walking paths.

**Travel Time and Cost Variables:** These variables represent the travel times and costs associated with different transportation modes and routes. The primary travel time and cost variables include:

**Travel Time:** It represents the time required to travel between different origin-destination pairs using different transportation modes or routes. Travel time is influenced by factors such as traffic congestion, travel speeds, transit schedules, and route characteristics.

**Travel Cost:** It represents the monetary cost or fare associated with different transportation modes or routes. Travel cost includes factors such as fuel costs, tolls, transit fares, parking fees, and other costs incurred during travel.

**Environmental Parameters:** These parameters represent the environmental impacts of transportation systems. The primary environmental parameters include:

**Emissions:** Parameters related to pollutant emissions from different transportation modes, such as carbon dioxide (CO<sub>2</sub>), nitrogen oxides (NO<sub>x</sub>), particulate matter (PM), and other pollutants.

**Energy Consumption:** Parameters related to energy consumption by different transportation modes, such as fuel consumption rates, energy efficiency, and energy demand.

**Sustainability Indicators:** Parameters related to sustainability criteria, such as greenhouse gas emissions, air quality, land use, noise pollution, and other indicators used to assess the environmental sustainability of transportation systems.

By considering these variables and parameters, transportation planners can analyze current transportation systems, forecast future transportation demands, evaluate infrastructure needs, develop transportation plans and policies, and assess the impacts of transportation interventions on travel behavior.

**Transport Economics:** Research in this area involves studying the economic aspects of transportation systems. It includes analyzing cost-benefit analysis, pricing mechanisms, investment evaluation, demand forecasting, and economic impacts of transportation projects and policies. The objective is to understand the economic implications of transportation decisions and identify efficient and sustainable solutions.

In the Transport Economics approach applied to transportation problems, various variables and parameters are considered to analyze the economic aspects of transportation systems. Here are the key variables and parameters typically considered:

**Demand Variables:** These variables represent the demand for transportation services and the behavior of transportation users. The primary demand variables include:

- **Quantity Demanded:** It represents the quantity of transportation services demanded by users, such as the number of trips, passenger-kilometers, or ton-kilometers.
- **Price Sensitivity:** It represents the responsiveness of transportation demand to changes in prices. Price sensitivity determines the elasticity of demand and helps analyze how demand changes with price variations.

- **Income Level:** It represents the income of transportation users, which influences their ability to afford transportation services. Income level affects the demand for different transportation modes and services.
- **User Preferences:** It represents the preferences of transportation users, including factors like convenience, comfort, travel time, reliability, and service quality. User preferences influence modal choices and demand patterns.

**Cost Variables:** These variables represent the costs associated with transportation services and infrastructure. The primary cost variables include:

- **Operating Costs:** It represents the costs incurred in providing transportation services, such as fuel costs, labor costs, maintenance costs, vehicle depreciation, insurance, and other operational expenses.
- **Infrastructure Costs:** It represents the costs associated with building and maintaining transportation infrastructure, including road construction, maintenance, public transit infrastructure, and other related expenses.
- **External Costs:** It represents the costs imposed on society but not directly borne by transportation providers or users, such as environmental costs, congestion costs, accidents, and health impacts. External costs are often considered to analyze the overall economic efficiency of transportation systems.

**Pricing and Revenue Variables:** These variables represent the pricing mechanisms and revenue generation in transportation systems. The primary pricing and revenue variables include:

- **Fare or Tariff Structure:** It represents the pricing structure for transportation services, including ticket fares, tolls, fees, and charges associated with different transportation modes and services.
- **Revenue Generation:** It represents the revenue generated from transportation services, which includes fare revenue, toll revenue, advertising revenue, and other sources of income for transportation providers.

**Investment and Financing Parameters:** These parameters represent the investment requirements and financing mechanisms for transportation infrastructure. The primary investment and financing parameters include:

- **Capital Investment:** It represents the investment needed for the construction, expansion, or maintenance of transportation infrastructure, including roads, bridges, tunnels, ports, airports, rail networks, and public transit systems.
- **Financing Mechanisms:** It represents the methods and sources of financing for transportation infrastructure projects, including public funding, private investment, public-private partnerships, toll financing, subsidies, and grants.

**Economic Evaluation Metrics:** These metrics represent the economic indicators used to evaluate transportation projects and policies. The primary economic evaluation metrics include:

- **Cost-Benefit Analysis:** It represents the comparison of the costs and benefits associated with transportation projects or policies. Cost-benefit analysis helps determine the economic viability and efficiency of transportation interventions.
- **Economic Impact Assessment:** It represents the assessment of the broader economic impacts of transportation projects, such as employment generation, income effects, productivity gains, and regional economic development.
- **Return on Investment (ROI):** It represents the financial return or profitability of transportation investments. ROI is used to evaluate the financial viability and attractiveness of transportation projects.
- **Value of Time:** It represents the economic value or utility that individuals assign to their travel time. Value of time is used to estimate the economic benefits of reducing travel time or improving travel conditions.

By considering these variables and parameters, transport economists analyze the economic efficiency, affordability, and sustainability of transportation systems, evaluate the impacts of transportation policies, and make recommendations for improving economic outcomes in the transportation sector.

**Transport Safety and Risk Analysis:** This type of research focuses on studying transportation safety, accident analysis, risk assessment, and developing strategies to mitigate risks and enhance safety measures. It involves analyzing factors that contribute to accidents, evaluating safety regulations, and designing interventions to improve road safety.

In the Transport Safety and Risk Analysis approach applied to transportation problems, various variables and parameters are considered to assess and manage the safety and risks associated with transportation systems. Here are the key variables and parameters typically considered:

**Accident Variables:** These variables represent the occurrences and characteristics of accidents or incidents in the transportation system. The primary accident variables include:

- **Accident Frequency:** It represents the number of accidents or incidents that occur within a given period in the transportation system.
- **Accident Severity:** It represents the level of severity or consequences of accidents, including factors such as injuries, fatalities, property damage, and environmental impacts.
- **Accident Types:** It represents the different types of accidents or incidents that occur in transportation, such as collisions, derailments, fires, hazardous material spills, or other specific types of incidents.
- **Contributing Factors:** It represents the factors that contribute to accidents, including human factors (e.g., driver behavior, fatigue), vehicle factors (e.g., mechanical failure), infrastructure factors (e.g., road design, signage), and environmental factors (e.g., weather conditions).

**Risk Variables:** These variables represent the assessment and analysis of risks associated with transportation systems. The primary risk variables include:

- **Risk Assessment:** It represents the evaluation of potential risks and hazards in the transportation system, considering the likelihood of occurrence and the consequences of incidents.
- **Risk Factors:** It represents the factors that contribute to the likelihood or severity of risks, such as exposure to hazardous conditions, vulnerability of road users, system vulnerabilities, or potential failures.
- **Risk Mitigation Measures:** It represents the strategies and measures implemented to reduce or mitigate risks in transportation systems, including safety regulations, infrastructure improvements, operational protocols, and safety technologies.

**Safety Performance Indicators:** These indicators represent the metrics used to measure and monitor safety performance in transportation systems. The primary safety performance indicators include:

- **Fatality Rate:** It represents the number of fatalities per unit of travel distance or time, indicating the safety level of the transportation system.
- **Injury Rate:** It represents the number of injuries per unit of travel distance or time, indicating the level of safety and potential risks in the transportation system.
- **Crash Rate:** It represents the number of crashes or accidents per unit of travel distance or time, providing insights into the frequency of incidents in the transportation system.

**Safety Interventions:** These interventions represent the measures and strategies implemented to enhance safety in transportation systems. The primary safety interventions include:

- **Infrastructure Safety Improvements:** Parameters related to the design, construction, and maintenance of transportation infrastructure to improve safety, such as road geometry, signage, traffic control devices, lighting, and visibility enhancements.
- **Vehicle Safety Technologies:** Parameters related to the integration of safety technologies in vehicles, such as seat belts, airbags, anti-lock braking systems (ABS), electronic stability control (ESC), collision avoidance systems, and advanced driver assistance systems (ADAS).
- **Education and Awareness Programs:** Parameters related to educational campaigns, driver training programs, public awareness initiatives, and community outreach efforts to promote safe transportation behavior and raise awareness about safety risks.
- **Enforcement and Regulations:** Parameters related to enforcing traffic laws and regulations, implementing safety standards, conducting inspections, and monitoring compliance

**Environmental and Sustainable Transportation:** Research in this area aims to address the environmental impacts of transportation systems and develop sustainable solutions. It involves studying emissions, energy consumption, pollution, alternative fuels, green transportation technologies, and promoting sustainable transportation practices.

In the Environmental and Sustainable Transportation approach applied to transportation problems, various variables and parameters are considered to assess and promote environmental sustainability in transportation systems. Here are the key variables and parameters typically considered:

Emissions and Pollution Variables: These variables represent the environmental impacts and emissions associated with transportation activities. The primary emissions and pollution variables include:

- Greenhouse Gas (GHG) Emissions: It represents the emissions of carbon dioxide (CO<sub>2</sub>), methane (CH<sub>4</sub>), nitrous oxide (N<sub>2</sub>O), and other GHGs that contribute to climate change and global warming.
- Air Pollutant Emissions: It represents the emissions of pollutants such as nitrogen oxides (NO<sub>x</sub>), particulate matter (PM), volatile organic compounds (VOCs), and other harmful substances that contribute to air pollution and have health and environmental impacts.
- Noise Pollution: It represents the noise generated by transportation activities, such as road traffic, aircraft, or railways, which can have adverse effects on human health and well-being.

Energy Efficiency Variables: These variables represent the energy consumption and efficiency of transportation systems. The primary energy efficiency variables include:

- Fuel Consumption: It represents the amount of fuel consumed by different transportation modes, such as gasoline, diesel, electricity, or alternative fuels.
- Energy Consumption: It represents the total energy consumed by transportation activities, including both fuel and electricity usage.
- Energy Efficiency: It represents the efficiency of energy use in transportation, considering factors such as vehicle technologies, operational practices, modal choices, and energy conservation measures.

Sustainable Practices and Parameters: These parameters represent the sustainable practices and considerations in transportation systems. The primary sustainable parameters include:

- Sustainable Modes: Parameters related to promoting and prioritizing sustainable transportation modes, such as walking, cycling, public transit, and other forms of low-carbon or active transportation.
- Transit-Oriented Development: Parameters related to the integration of transportation infrastructure with land use planning, promoting compact and mixed-use developments around transit nodes to reduce travel distances and encourage sustainable travel patterns.



- **Vehicle Technologies:** Parameters related to promoting and adopting low-emission and energy-efficient vehicle technologies, such as electric vehicles (EVs), hybrid vehicles, hydrogen fuel cells, and other alternative fuel vehicles.
- **Infrastructure Sustainability:** Parameters related to sustainable infrastructure design and practices, such as using eco-friendly construction materials, incorporating green infrastructure elements, promoting energy-efficient traffic management systems, and utilizing renewable energy sources.

**Life Cycle Assessment (LCA):** Life Cycle Assessment is a methodology used to assess the environmental impacts of transportation systems throughout their life cycle, including the production, operation, and disposal phases. LCA considers factors such as raw material extraction, manufacturing processes, energy consumption, emissions, and waste generation to evaluate the overall sustainability of transportation systems.

**Policy and Regulatory Instruments:** These instruments represent the policies, regulations, and incentives implemented to promote environmental and sustainable transportation practices.

The primary policy and regulatory instruments include:

- **Emission Standards:** Regulations and standards that impose limits on emissions from vehicles and transportation activities, encouraging the use of cleaner technologies and fuels.
- **Fuel Efficiency Standards:** Regulations that set requirements for the energy efficiency and fuel consumption of vehicles, promoting the development and adoption of fuel-efficient technologies.
- **Carbon Pricing:** Policies that put a price on carbon emissions, such as carbon taxes or cap-and-trade systems, to incentivize emission reductions and encourage sustainable transportation choices.
- **Sustainable Transport Planning:** Policies and guidelines that promote sustainable transportation planning practices, including the integration of environmental considerations, public participation, and the use of sustainable transportation indicators.

By considering these variables and parameters, transportation planners and policymakers can assess the environmental impacts of transportation systems, identify opportunities for improvement, promote sustainable practices, and develop policies and strategies to mitigate environmental harm and

**Human Factors and Transportation Behavior:** This type of research focuses on understanding human behavior and decision-making in transportation systems. It involves studying factors that influence travel choices, transportation mode preferences, travel behavior patterns, and user satisfaction. The objective is to design user-centric transportation systems and policies that meet the needs and preferences of individuals.

In the Human Factors and Transportation Behavior approach applied to transportation problems, various variables and parameters are considered to understand and analyze the behavior of individuals and groups in transportation systems. Here are the key variables and parameters typically considered:

**Travel Behavior Variables:** These variables represent the choices and preferences of individuals in their travel behavior. The primary travel behavior variables include:

- **Mode Choice:** It represents the selection of transportation modes for travel, such as private vehicles, public transit, walking, cycling, or other modes.
- **Route Choice:** It represents the selection of specific routes or paths within a transportation network, considering factors such as travel time, distance, congestion levels, and perceived safety.
- **Trip Chaining:** It represents the sequencing and combination of multiple activities or destinations within a single trip, considering factors such as convenience, efficiency, and accessibility.
- **Time of Travel:** It represents the timing and scheduling of travel activities, including factors such as peak-hour congestion, work schedules, school timings, and other temporal considerations.

**Individual Characteristics:** These characteristics represent the attributes and traits of individuals that influence their transportation behavior. The primary individual characteristics include:

- **Demographics:** Parameters such as age, gender, income, education level, occupation, and household composition that influence travel patterns and preferences.
- **Attitudes and Perceptions:** Parameters related to individuals' attitudes, beliefs, values, and perceptions about transportation modes, safety, comfort, convenience, environmental impacts, and other relevant factors.

- **Mobility Needs and Constraints:** Parameters related to individuals' mobility requirements and constraints, such as accessibility to transportation options, physical limitations, mobility impairments, or financial constraints.
- **Travel Experience:** Parameters related to individuals' past travel experiences, familiarity with transportation networks, and previous encounters with transportation services or modes.

**Psychological Factors:** These factors represent the psychological aspects that influence transportation behavior. The primary psychological factors include:

- **Risk Perception:** It represents how individuals perceive and evaluate risks associated with different transportation modes, routes, or activities, affecting their mode and route choices.
- **Habit and Routine:** Parameters related to the habits, routines, and established travel patterns of individuals, which may influence their resistance to behavior change or adoption of new transportation options.
- **Cognitive Factors:** Parameters related to cognitive processes, decision-making, information processing, and judgment that affect individuals' transportation choices and behavior.
- **Emotional Factors:** Parameters related to individuals' emotions, preferences, and affective responses associated with transportation modes, routes, or travel experiences.

**Social Factors:** These factors represent the social influences on transportation behavior. The primary social factors include:

- **Social Norms:** Parameters related to societal expectations, cultural norms, and social influences that shape individuals' transportation choices and behavior.
- **Peer Influence:** Parameters related to the influence of friends, family, colleagues, and social networks on individuals' transportation decisions and behavior.
- **Social Equity:** Parameters related to accessibility and equity considerations, such as the availability of transportation options for disadvantaged populations, access to essential services, and transportation-related social justice issues.

**Information and Communication:** These parameters represent the role of information and communication technologies in transportation behavior. The primary information and communication parameters include:

- **Travel Information:** Parameters related to the availability and accessibility of travel-related information, such as real-time traffic updates, transit schedules, route guidance, and travel planning tools.
- **Communication Channels:** Parameters related to the communication channels and platforms used for disseminating transportation information, such as mobile apps, websites, social media, or traditional media.
- **Information Accessibility:** Parameters related to the inclusiveness and accessibility of transportation information for different user groups, including individuals with disabilities or limited access to technology.
- **User Interfaces:** Parameters related to the design and usability of transportation information systems.

## 6. Transportation And Vehicle Routing Problem

Transportation plays a crucial role in our daily lives and is a fundamental component of economic activities. It involves the movement of people and goods from one location to another using various modes of transportation, such as road, rail, air, and water. Efficient transportation systems are essential for ensuring the smooth functioning of supply chains, facilitating trade, and promoting economic growth.

Within the realm of transportation, the Vehicle Routing Problem (VRP) is a well-studied and significant optimization challenge. The VRP seeks to determine the most efficient routes and schedules for a fleet of vehicles to serve a set of customers while minimizing costs or maximizing certain objectives. It is a complex combinatorial optimization problem with numerous practical applications in logistics, distribution, and transportation management [19],[20], [21],[22].

The VRP involves a set of customers with specific demands or deliveries to be made. Each customer has a location, a demand for goods or services, and sometimes time windows within which they must be served. The objective is to assign the customers to vehicles, determine the optimal routes for each vehicle, and schedule the deliveries to minimize total travel distance, time, or other cost-related factors.

There are several variants of the VRP, each introducing additional constraints and considerations:

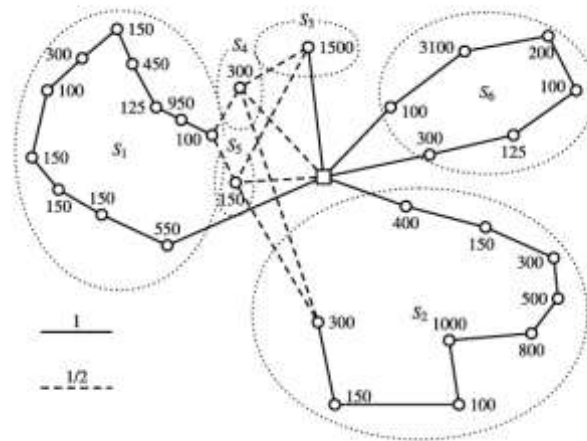


Fig.1- General conceptual form of VRP

Capacitated Vehicle Routing Problem (CVRP): In this variant, vehicles have limited carrying capacities, and the total demand of customers served by each vehicle must not exceed this capacity.

Vehicle Routing Problem with Time Windows (VRPTW): Here, each customer has a specific time window within which they can be served. The objective is to complete all deliveries within the given time windows while optimizing other factors like travel distance or vehicle utilization.

Vehicle Routing Problem with Pickup and Delivery (VRPPD): This variant involves pickups and deliveries where vehicles are required to pick up goods from certain locations before delivering them to customers.

Electric Vehicle Routing Problem (EVRP): The EVRP considers the limited range and recharging requirements of electric vehicles, aiming to optimize routes while considering charging station locations and recharge times.

Solving the VRP is a complex task due to its combinatorial nature and the need to consider multiple objectives and constraints. Researchers and practitioners have developed various algorithms and techniques to address the VRP, including exact methods like branch-and-bound and dynamic programming, as well as metaheuristic approaches such as genetic algorithms, simulated annealing, and ant colony optimization.

Efficient solutions to the VRP can result in significant cost savings, reduced travel time, improved resource utilization, and environmental benefits. The application of advanced optimization techniques and real-time data in transportation management systems has further enhanced the effectiveness of VRP solutions, enabling companies to streamline their operations, reduce fuel consumption, and improve customer satisfaction.

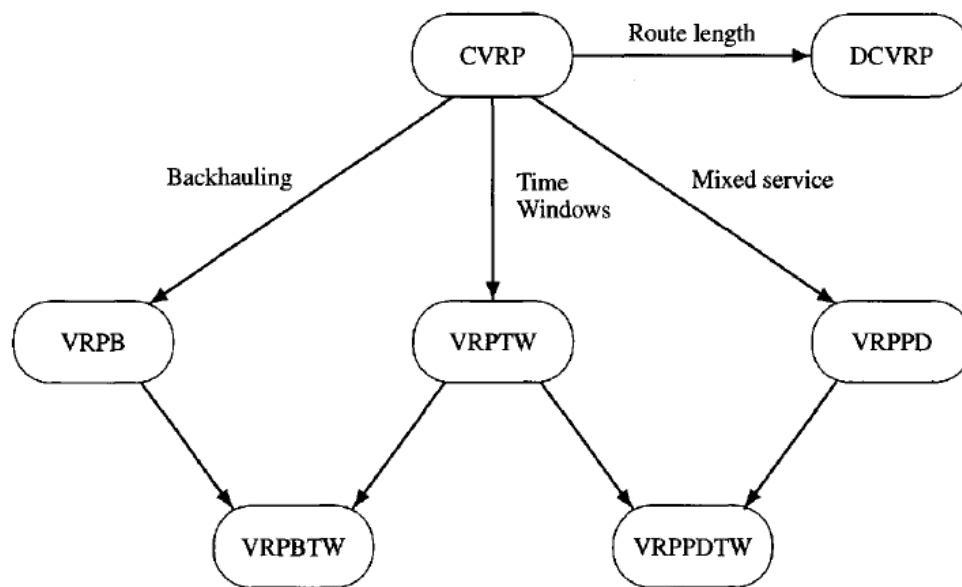


Fig.2-The basic problems of the VRP class and their interconnections.

Overall, the Vehicle Routing Problem is a critical area of research and practical application in transportation and logistics. Its optimization can lead to more efficient and sustainable transportation systems, benefiting businesses, consumers, and the environment.

Approaches for solving the Vehicle Routing Problem (VRP) can be categorized into different groups based on the solution methods and techniques employed. Here are some common categories:

**Exact Methods:** These approaches aim to find the optimal solution by exhaustively exploring the solution space. Examples of exact methods include:

- a. Integer Programming (IP): Formulating the VRP as a mathematical optimization problem and solving it using IP techniques.
- b. Branch and Bound: Employing a divide-and-conquer strategy to explore the search space efficiently and find the optimal solution.

**Heuristic Methods:** Heuristic approaches provide good-quality solutions in a reasonable amount of time by employing approximation techniques. They are often faster than exact methods but may not guarantee optimality. Some heuristic methods for the VRP include:

- a. **Construction Heuristics:** Building initial solutions by sequentially assigning customers to vehicles based on certain rules or heuristics.
- b. **Local Search:** Iteratively improving an initial solution by making small modifications to the routes and evaluating their impact on the objective function.
- c. **Savings Algorithm:** Assigning customers to routes based on the savings obtained from combining two customers' routes into a single route.

**Metaheuristic Methods:** Metaheuristics are high-level strategies that guide the search process in the solution space. They can be used to find good-quality solutions within a reasonable amount of time. Some common metaheuristic methods for the VRP include:

- a. **Genetic Algorithms (GA):** Inspired by the principles of biological evolution, GA uses genetic operators like selection, crossover, and mutation to explore the search space.
- b. **Ant Colony Optimization (ACO):** Mimicking the foraging behavior of ants, ACO uses pheromone trails to guide the search process and find promising routes.
- c. **Simulated Annealing:** Inspired by the annealing process in metallurgy, this method uses a probabilistic acceptance criterion to escape local optima and search for better solutions.

**Hybrid Methods:** Hybrid approaches combine multiple solution methods to leverage their strengths and mitigate their weaknesses. These methods often combine exact and heuristic/metaheuristic techniques to find high-quality solutions efficiently.

**Problem-Specific Methods:** Some approaches are tailored to specific VRP variants or problem characteristics. These methods exploit the problem's unique structure and constraints to design specialized algorithms that can provide efficient solutions.

It's important to note that the categorization above is not exhaustive, and there may be other specific approaches or variations within each category. The choice of approach depends on factors such as problem size, complexity, available computational resources, and the trade-off between solution quality and computation time.

## 7. Transportation And Vehicle Routing Problem And Time Windows

Transportation is the process of moving people, goods, or resources from one location to another. It plays a vital role in various industries, supply chains, and everyday life. Efficient transportation systems are essential for economic development, trade, and social connectivity.

Within transportation, the Vehicle Routing Problem (VRP) is a significant optimization challenge. The VRP focuses on determining optimal routes and schedules for a fleet of vehicles to serve a set of customers or locations. It aims to minimize costs, maximize efficiency, or achieve specific objectives while considering various constraints and factors.

One important variant of the VRP is the Vehicle Routing Problem with Time Windows (VRPTW). In VRPTW, each customer or location has a specific time window during which they can be served or receive deliveries. These time windows represent the availability or preferred time slots for service. The objective is to design routes and schedules that respect these time windows and complete all deliveries within the given constraints. The inclusion of time windows in the VRP adds an additional layer of complexity and realism to the problem. It reflects practical considerations such as customer preferences, operational constraints, and the need to optimize resource utilization. By incorporating time windows, the VRPTW aims to ensure timely deliveries, reduce waiting times, and improve overall service quality.

Effectively solving the VRPTW requires algorithms and techniques that can handle the time-related constraints and optimize routes accordingly. Several approaches have been developed, including exact methods, heuristics, and metaheuristic algorithms. These techniques consider factors like travel time, vehicle capacity, customer priorities, and time window violations to generate optimal or near-optimal solutions [23], [24], [25], [26], [27],

The benefits of solving the VRPTW efficiently include improved customer satisfaction, reduced transportation costs, optimized resource allocation, and increased operational efficiency. By respecting time windows, companies can provide reliable and punctual services, enhance their reputation, and gain a competitive edge in the market.

Moreover, the VRPTW is particularly relevant in industries such as delivery services, e-commerce, retail, and logistics, where timely and efficient deliveries are critical. It enables companies to



better manage their fleet, allocate resources effectively, minimize delays, and streamline their operations.

In recent years, advancements in technology and data availability have further enhanced the capabilities of VRPTW solutions. Real-time data on traffic conditions, weather, and customer preferences can be integrated into the optimization process, allowing for dynamic and adaptive routing decisions. This enables companies to respond to changing conditions, optimize routes in real-time, and provide more accurate estimated arrival times to customers.

In summary, the Vehicle Routing Problem with Time Windows (VRPTW) addresses the challenge of optimizing routes and schedules while respecting customer-specific time windows. It is an essential problem in transportation and logistics, with practical applications in various industries. Efficient solutions to the VRPTW lead to improved customer service, reduced costs, and enhanced operational efficiency for businesses.

## **8. Vehicle Routing Problem and time windows relations and challenges:**

In the VRP, the concept of "window time" refers to time constraints or time windows associated with customer visits. Each customer has a specified time window within which the vehicle must arrive to serve them. The time window consists of an earliest arrival time (earliest time the vehicle can arrive) and a latest arrival time (latest time the vehicle can arrive). It represents the operational constraints or service requirements of the customers.

The relation between the VRP and time windows is that the VRP with time windows extends the basic VRP formulation by incorporating time constraints for customer visits. In the traditional VRP, there are no specific time constraints, and the goal is typically to minimize the total distance traveled. However, in real-world scenarios, customers often have specific time requirements or operational constraints that need to be satisfied [28], [29], [30].

The introduction of time windows in the VRP adds an additional level of complexity to the problem. It requires the optimization algorithm to consider not only the vehicle routes and distances but also the timing of customer visits. The algorithm must ensure that each customer is served within their specified time window. If a vehicle arrives too early or too late, it may lead to customer dissatisfaction or penalties.

The presence of time windows in the VRP introduces challenges such as:

**Time Window Violations:** The algorithm needs to find feasible routes that respect the time windows of all customers. This means ensuring that the vehicle arrives within the specified time window for each customer while still optimizing the overall objective function.

**Time Window Tightness:** Different customers may have different levels of time window flexibility. Some customers may have tight time windows, requiring precise arrival times, while others may have more lenient time windows. The algorithm must consider these variations and adapt accordingly.

**Time Window Overlaps:** In some cases, time windows of different customers may overlap, meaning that a vehicle can serve multiple customers within the same time window. The algorithm must identify and exploit such opportunities to improve efficiency.

Efficiently incorporating time windows into the VRP requires the use of advanced optimization techniques and algorithms specifically designed for the VRP with time windows. These algorithms consider the interplay between vehicle routes, distances, and the timing of customer visits to find optimal or near-optimal solutions that satisfy the time window constraints while minimizing overall costs or distances traveled.

Planning in the field of Vehicle Routing Problem (VRP) with time windows faces several limitations that can affect the effectiveness and efficiency of the solutions. Some of the key limitations include:

**Complexity:** The VRP with time windows is a highly complex problem, especially when dealing with large-scale instances. As the number of customers, vehicles, and time windows increases, the problem's computational complexity grows exponentially. Finding optimal or near-optimal solutions within a reasonable time frame becomes increasingly challenging.

**Lack of Perfect Information:** Planning in VRP often relies on available data and assumptions, which may not capture the complete picture of the real-world conditions. Uncertainty in customer demands, traffic patterns, and other factors can impact the accuracy of the planning process. Limited or imperfect information can lead to suboptimal routing decisions and inefficiencies.

**Static Time Windows:** Traditional approaches to VRP with time windows assume static time windows that do not change throughout the planning horizon. However, time windows can be subject to variations due to customer preferences, seasonality, traffic conditions, or other factors. Ignoring dynamic time windows can lead to inefficient routes and missed delivery opportunities.

**Lack of Flexibility:** VRP planning often focuses on generating fixed schedules and routes for vehicles. However, operational disruptions, such as traffic congestion, vehicle breakdowns, or unexpected delays, can impact the planned routes. Lack of flexibility in the planning process hinders the ability to adapt to changing circumstances and optimize routes in real-time.

**Limited Consideration of Constraints:** VRP planning must consider various constraints, such as vehicle capacities, driver working hours, delivery time windows, and other operational constraints. However, incorporating all these constraints simultaneously can be challenging. Simplified models or assumptions may be used to handle these constraints, which can result in suboptimal solutions.

**Trade-offs between Objectives:** VRP planning often involves multiple objectives, such as minimizing distance traveled, reducing costs, and optimizing customer service levels. However, these objectives can be conflicting, making it difficult to find a single optimal solution. Balancing these objectives requires making trade-offs, and finding the right balance can be a complex task.

**Lack of Real-Time Adaptability:** Traditional VRP planning often operates in a static, offline mode, without the ability to adapt to real-time changes. While real-time data and technologies exist, incorporating them into the planning process can be challenging. The lack of real-time adaptability limits the ability to optimize routes dynamically and respond to unforeseen events or disruptions.

Overcoming these limitations requires advancements in algorithms, optimization techniques, and decision support systems. Incorporating real-time data, considering dynamic time windows, and developing adaptive planning strategies can help address these limitations and improve the effectiveness of VRP planning with time windows [30].

## 9. The Famous Models About Solving Vehicle Routing And Time Windows Problem

There are several famous models and algorithms that have been developed to solve the Vehicle Routing Problem (VRP) with time windows. Here are some of the notable ones:

**Clarke and Wright Savings Algorithm:** Although originally developed for the basic VRP without time windows, this algorithm has been extended to handle time-constrained problems. It is a constructive heuristic that starts with an initial solution based on the savings concept and then iteratively improves the routes by merging and re-optimizing them.

**Sweep Algorithm:** This algorithm is another heuristic approach that constructs initial solutions by dividing the customers into sectors based on their geographical positions and then applying a sweeping process to create routes. It has been adapted to handle time window constraints by incorporating them into the route construction process.

**Time-Window Exchange Algorithm:**

This algorithm focuses on improving existing solutions by exchanging customers between routes while respecting their time windows. It applies a local search strategy to iteratively swap customers between routes to improve the overall objective function and satisfy time window constraints. **Vehicle Routing Problem with Time Windows and Split Deliveries (VRPTWSD):** This model extends the VRP with time windows by allowing multiple visits or split deliveries to the same customer within their time window. It addresses the scenario where a customer may require multiple deliveries or pickups during a specific period.

**Time-Dependent VRP (TDVRP):** The TDVRP considers the dynamic nature of travel times and incorporates time-dependent travel costs or time-dependent customer demands. It considers factors such as traffic congestion, time-of-day variations, and other temporal factors that affect travel times and customer service times [31].

**Sequential Insertion Heuristic:** This approach sequentially inserts customers into routes based on their time windows and cost criteria. It iteratively selects the next customer to insert based on specific rules or heuristics, such as the nearest neighbor or best insertion [32].

Metaheuristic Approaches: Various metaheuristic algorithms, such as Genetic Algorithms (GA), Ant Colony Optimization (ACO), and Particle Swarm Optimization (PSO), have been applied to the VRP with time windows. These algorithms use iterative optimization techniques inspired by natural phenomena to find near-optimal solutions [33].

It's worth noting that the field of VRP research is vast, and numerous variations and hybrid approaches exist to solve specific problem instances or incorporate additional constraints. The selection of a particular model or algorithm depends on factors such as problem size, complexity, time window characteristics, and specific objectives or constraints of the transportation problem at hand.

## 10. Conclusion

In conclusion, the Vehicle Routing Problem (VRP) is a significant and challenging optimization problem in the field of logistics and transportation. It involves determining the optimal routes and schedules for a fleet of vehicles to serve a set of customers or locations while considering various constraints and objectives.

The VRP has been extensively studied, and numerous models, algorithms, and approaches have been developed to tackle different variations and real-world complexities. These models and algorithms range from classical heuristics to sophisticated metaheuristic techniques, each with its own strengths and limitations. Efficiently solving the VRP has practical implications in various industries, including transportation, delivery services, and supply chain management. By optimizing vehicle routes, the VRP can lead to significant cost savings, improved customer service, reduced fuel consumption, and lower environmental impacts.

The VRP is a versatile problem that can be extended to incorporate additional constraints such as time windows, split deliveries, dynamic travel times, and other factors relevant to specific real-world scenarios. Researchers continue to explore new algorithms and techniques to address these extensions and advance the state-of-the-art in solving the VRP. However, despite the progress made, the VRP remains a challenging problem due to its combinatorial nature and the complexity of real-world transportation networks. Further research is needed to develop more efficient algorithms, hybrid approaches, and advanced optimization techniques to handle larger problem instances and incorporate additional constraints.

In conclusion, the VRP represents a crucial area of study with practical implications and ongoing research efforts. By continuously advancing our understanding and solving capabilities for the VRP, we can contribute to more efficient and sustainable transportation systems, benefiting both businesses and society.

## References:

1. Dempsey, P. S. (2002). Transportation: A legal history. *Transp. LJ*, 30, 235.
2. Herbst, J. (2005). *The history of transportation*. Lerner Publications.
3. [3] Goel, A., & Gruhn, V. (2008). A general vehicle routing problem. *European Journal of Operational Research*, 191(3), 650-660.
4. [4] R. Baldacci, E. Bartolini, and G. Laporte, Some applications of the generalized vehicle routing problem, *Journal of the Operational Research Society*, 61 (2010), pp. 1072–1077.
5. [5] H. Andersson, A. Hoff, M. Christiansen, G. Hasle, and A. Lokketangen, Industrial aspects and literature survey: Combined inventory management and routing, *Computers & Operations Research*, 37 (2010), pp. 1515–1536.
6. [6] C. Archetti and M. G. Speranza, Vehicle routing problems with split deliveries, *International Transactions in Operational Research*, 19 (2012), pp. 3–22.
7. [7] C. Archetti and M. G. Speranza, A survey on matheuristics for routing problems, *EURO, Journal on Computational Optimization*, 2 (2014), pp. 223–246.
8. [8] Schrijver, A. (2002). On the history of the transportation and maximum flow problems. *Mathematical programming*, 91, 437-445.
9. [9] Meyer, B. H. (1917). *History of Transportation in the United States before 1860* (Vol. 215). Carnegie Institution of Washington.
10. [10] Biljecki, F., Ledoux, H., & Van Oosterom, P. (2013). Transportation mode-based segmentation and classification of movement trajectories. *International Journal of Geographical Information Science*, 27(2), 385-407.
11. [11] Saki, M., Abolhasan, M., & Lipman, J. (2019). A novel approach for big data classification and transportation in rail networks. *IEEE Transactions on Intelligent Transportation Systems*, 21(3), 1239-1249.
12. [12] Fang, S. H., Liao, H. H., Fei, Y. X., Chen, K. H., Huang, J. W., Lu, Y. D., & Tsao, Y. (2016). Transportation modes classification using sensors on smartphones. *Sensors*, 16(8), 1324.
13. [13] Shin, D., Aliaga, D., Tunçer, B., Arisona, S. M., Kim, S., Zünd, D., & Schmitt, G. (2015). Urban sensing: Using smartphones for transportation mode classification. *Computers, Environment and Urban Systems*, 53, 76-86.

15. [14] Gupta, A., Gupta, H. P., Biswas, B., & Dutta, T. (2020). An early classification approach for multivariate time series of on-vehicle sensors in transportation. *IEEE Transactions on Intelligent Transportation Systems*, 21(12), 5316-5327.
16. [15] Brilon, W. (2000, July). Traffic flow analysis beyond traditional methods. In *Proceedings of the 4th International Symposium on Highway Capacity* (pp. 26-41). Washington, DC, USA: Transportation Research Board.
17. [16] Kashinath, S. A., Mostafa, S. A., Mustapha, A., Mahdin, H., Lim, D., Mahmoud, M. A., ... & Yang, T. J. (2021). Review of data fusion methods for real-time and multi-sensor traffic flow analysis. *IEEE Access*, 9, 51258-51276.
18. [17] Brown, M. A. (2006). Traffic control howto. *Guide to IP Layer Network*, 49, 36.
19. [18] Mitsakis, E., Salanova, J. M., & Giannopoulos, G. (2011). Combined dynamic traffic assignment and urban traffic control models. *Procedia-Social and Behavioral Sciences*, 20, 427-436.
20. [19] Toth, P., & Vigo, D. (2002). An overview of vehicle routing problems. *The vehicle routing problem*, 1-26.
21. [20] Garaix, T., Artigues, C., Feillet, D., & Josselin, D. (2010). Vehicle routing problems with alternative paths: An application to on-demand transportation. *European Journal of Operational Research*, 204(1), 62-75.
22. [21] Gracia, C., Velázquez-Martí, B., & Estornell, J. (2014). An application of the vehicle routing problem to biomass transportation. *Biosystems engineering*, 124, 40-52.
23. [22] Kuo, Y. (2010). Using simulated annealing to minimize fuel consumption for the time-dependent vehicle routing problem. *Computers & Industrial Engineering*, 59(1), 157-165.
24. [23] Schneider, M., Stenger, A., & Goeke, D. (2014). The electric vehicle-routing problem with time windows and recharging stations. *Transportation science*, 48(4), 500-520.
25. [24] Liu, C., Kou, G., Zhou, X., Peng, Y., Sheng, H., & Alsaadi, F. E. (2020). Time-dependent vehicle routing problem with time windows of city logistics with a congestion avoidance approach. *Knowledge-Based Systems*, 188, 104813.
26. [25] Zulvia, F. E., Kuo, R. J., & Nugroho, D. Y. (2020). A many-objective gradient evolution algorithm for solving a green vehicle routing problem with time windows and time dependency for perishable products. *Journal of Cleaner Production*, 242, 118428.
27. [26] Spliet, R., Dabia, S., & Van Woensel, T. (2018). The time window assignment vehicle routing problem with time-dependent travel times. *Transportation Science*, 52(2), 261-276.

28. [27] Niu, Y., Yang, Z., Chen, P., & Xiao, J. (2018). Optimizing the green open vehicle routing problem with time windows by minimizing comprehensive routing cost. *Journal of cleaner production*, 171, 962-971.
29. [28] Demir, E., Huckle, K., Syntetos, A., Lahy, A., & Wilson, M. (2019). Vehicle routing problem: Past and future. *Contemporary Operations and Logistics: Achieving Excellence in Turbulent Times*, 97-117.
30. [29] Falkner, J. K., & Schmidt-Thieme, L. (2020). Learning to solve vehicle routing problems with time windows through joint attention. arXiv preprint arXiv:2006.09100.
31. [30] Gutierrez-Rodríguez, A. E., Conant-Pablos, S. E., Ortiz-Bayliss, J. C., & Terashima-Marín, H. (2019). Selecting meta-heuristics for solving vehicle routing problems with time windows via meta-learning. *Expert Systems with Applications*, 118, 470-481.
32. [31] Auer, A., Feese, S., Lockwood, S., & Hamilton, B. A. (2016). *History of intelligent transportation systems* (No. FHWA-JPO-16-329). United States. Department of Transportation. Intelligent Transportation Systems Joint Program Office.
33. [32] Alfaseeh, L., & Farooq, B. (2020). Multi-factor taxonomy of eco-routing models and future outlook. *Journal of Sensors*, 2020.
34. [33] Omidinasab, F., & Goodarzimehr, V. (2020). A hybrid particle swarm optimization and genetic algorithm for truss structures with discrete variables. *Journal of Applied and Computational Mechanics*, 6(3), 593-604.